

Example with SPECK algorithm

Figure 1 shows the example of data in a small pyramid structure, of the type resulting from an image wavelet position, that was used by J.M. Shapiro in his paper “Embedded Image Coding Using Zerotrees of Wavelet Coefficients” *Transactions on Signal Processing*, vol. 41, Dec. 1993, to describe his EZW image coding algorithm.

	0	1	2	3	4	5	6	7
0	63	-34	49	10	7	13	-12	7
1	-31	23	14	-13	3	4	6	-1
2	15	14	3	-12	5	-7	3	9
3	-9	-7	-14	8	4	-2	3	2
4	-5	9	-1	47	4	6	-2	2
5	3	0	-3	2	3	-2	0	4
6	2	-3	6	-4	3	6	3	6
7	5	11	5	6	0	3	-4	4

Figure 1: Set of image wavelet coefficients used by example. The numbers outside the box indicate the set of co-ordinates.

Notational conventions:

- $S^k(i, j)$ under Point or Set denotes $2^k \times 2^k$ set with (i, j) upper left corner co-ordinate.
- $(i, j)\mathbf{k}$ under Control Lists denotes $2^k \times 2^k$ set with (i, j) upper left corner co-ordinate.
- (i, j) in LSP always a single point.

Comment	Point or Set	Output Bit	Action	Control Lists
n=5 Sorting $\mathcal{S}=S^1(0,0)$, $\mathcal{I} = \text{rest}$				LIS = $\{(0,0)\mathbf{1}\}$ LSP = ϕ
	$S^1(0,0)$	1	quad split, add to LIS(0)	LIS = $\{(0,0)\mathbf{0},(0,1)\mathbf{0},(1,0)\mathbf{0},(1,1)\mathbf{0}\}$ LSP = ϕ
	(0,0)	1+	(0,0) to LSP	LIS = $\{(0,1)\mathbf{0},(1,0)\mathbf{0},(1,1)\mathbf{0}\}$ LSP = $\{(0,0)\}$
	(0,1)	1-	(0,1) to LSP	LIS = $\{(1,0)\mathbf{0},(1,1)\mathbf{0}\}$ LSP = $\{(0,0),(0,1)\}$
	(1,0)	0	none	
	(1,1)	0	none	
Test \mathcal{I}	$\mathcal{S}(\mathcal{I})$	1	split to 3 \mathcal{S} 's, new \mathcal{I}	
	$S^1(0,2)$	1	quad split, add to LIS(0)	LIS = $\{(1,0)\mathbf{0},(1,1)\mathbf{0}\},(0,2)\mathbf{0},(0,3)\mathbf{0}\}(1,2)\mathbf{0},(1,3)\mathbf{0}$
	(0,2)	1+	(0,2) to LSP	LSP = $\{(0,0),(0,1),(0,2)\}$ LIS = $\{(1,0)\mathbf{0},(1,1)\mathbf{0}\},(0,3)\mathbf{0}\}(1,2)\mathbf{0},(1,3)\mathbf{0}$
	(0,3)	0	none	
	(1,2)	0	none	
	(1,3)	0	none	
	$S^1(2,0)$	0	add to LIS(1)	LIS = $\{(1,0)\mathbf{0},(1,1)\mathbf{0}\},(0,3)\mathbf{0}\}(1,2)\mathbf{0},(1,3)\mathbf{0},(2,0)\mathbf{0},(2,1)\mathbf{0}$
	$S^1(2,2)$	0	add to LIS(1)	LIS = $\{(1,0)\mathbf{0},(1,1)\mathbf{0}\},(0,3)\mathbf{0}\}(1,2)\mathbf{0},(1,3)\mathbf{0},(2,0)\mathbf{0},(2,1)\mathbf{0},(2,2)\mathbf{0}$
Test \mathcal{I}	$\mathcal{S}(\mathcal{I})$	1	split to 3 \mathcal{S} 's	
	$S^2(0,4)$	0	add to LIS(2)	LIS = $\{(1,0)\mathbf{0},(1,1)\mathbf{0}\},(0,3)\mathbf{0}\}(1,2)\mathbf{0},(1,3)\mathbf{0},(2,0)\mathbf{0},(2,1)\mathbf{0},(2,2)\mathbf{0},(2,3)\mathbf{0}$
	$S^2(4,0)$	1	quad split, add to LIS(1)	LIS = $\{(1,0)\mathbf{0},(1,1)\mathbf{0},(0,3)\mathbf{0},(1,2)\mathbf{0},(1,3)\mathbf{0},(2,0)\mathbf{0},(2,1)\mathbf{0},(2,2)\mathbf{0},(2,3)\mathbf{0}\}$
	$S^1(4,0)$	0	none	
	$S^1(4,2)$	1	quad split, add to LIS(0)	LIS = $\{(1,0)\mathbf{0},(1,1)\mathbf{0},(0,3)\mathbf{0},(1,2)\mathbf{0},(1,3)\mathbf{0},(4,0)\mathbf{1},(4,2)\mathbf{1},(6,0)\mathbf{1},(6,2)\mathbf{1},(0,4)\mathbf{2}\}$
	(4,2)	0	none	
	(4,3)	1+	move (4,3) to LSP	LSP = $\{(0,0),(0,1),(0,2),(4,3)\}$ LIS = $\{(1,0)\mathbf{0},(1,1)\mathbf{0},(0,3)\mathbf{0}\}(1,2)\mathbf{0},(1,3)\mathbf{0},(4,2)\mathbf{1},(6,0)\mathbf{1},(6,2)\mathbf{1},(0,4)\mathbf{2}$
	(5,2)	0	none	
	(5,3)	0	none	
	$S^1(6,0)$	0	none	
	$S^1(6,2)$	0	none	
End n=5 Sorting	$S^2(4,4)$	0	add to LIS(2)	LIS = $\{(1,0)\mathbf{0},(1,1)\mathbf{0},(0,3)\mathbf{0},(1,2)\mathbf{0},(1,3)\mathbf{0},(4,2)\mathbf{1},(6,0)\mathbf{1},(6,2)\mathbf{1},(0,4)\mathbf{2},(4,4)\mathbf{2}\}$ LSP = $\{(0,0),(0,1),(0,2),(4,3)\}$

Comment	Point or Set Tested	Output Bit	Action	Control Lists
n=4 Sorting				LIS = $\{(1,0)\mathbf{0},(1,1)\mathbf{0},(0,3)\mathbf{0},(1,2)\mathbf{0},(1,3)\mathbf{0},(4,2)\mathbf{1},(6,0)\mathbf{1},(6,2)\mathbf{1},(0,4)\mathbf{2},(4,4)\mathbf{2}\}$ LSP = $\{(0,0),(0,1),(0,2),(4,3)\}$
Test LIS(0)	(1,0)	1-	(1,0) to LSP	
	(1,1)	1+	(1,1) to LSP	LIS = $\{(0,3)\mathbf{0},(1,2)\mathbf{0},(1,3)\mathbf{0},(4,2)\mathbf{0},(5,2)\mathbf{0},(4,2)\mathbf{1},(6,0)\mathbf{1},(6,2)\mathbf{1},(0,4)\mathbf{2},(4,4)\mathbf{2}\}$ LSP = $\{(0,0),(0,1),(0,2),(4,3),(1,0),(1,1)\}$
	(0,3)	0	none	
	(1,2)	0	none	
	(1,3)	0	none	
	(4,2)	0	none	
	(5,2)	0	none	
	(5,3)	0	none	
Test LIS(1)	$S^1(2,0)$	0	none	
	$S^1(2,2)$	0	none	
	$S^1(4,0)$	0	none	
	$S^1(6,0)$	0	none	
	$S^1(6,2)$	0	none	
Test LIS(2)	$S^2(0,4)$	0	none	
	$S^2(4,4)$	0	none	
Refinement	(0,0)	1	decoder adds 2^4	
	(0,1)	0	decoder subtracts 0	
	(0,2)	1	decoder adds 2^4	
	(4,3)	0	decoder adds 0	
End n=4				